

a.) $V_{ab} = ?$ First, ... find the current in the outer loop.

$$\sum V_i = 0 \Rightarrow \sum V_i = -8V + 12V - (9\Omega)I = 0$$

$$I = \frac{4 \text{ volts}}{9 \Omega}$$

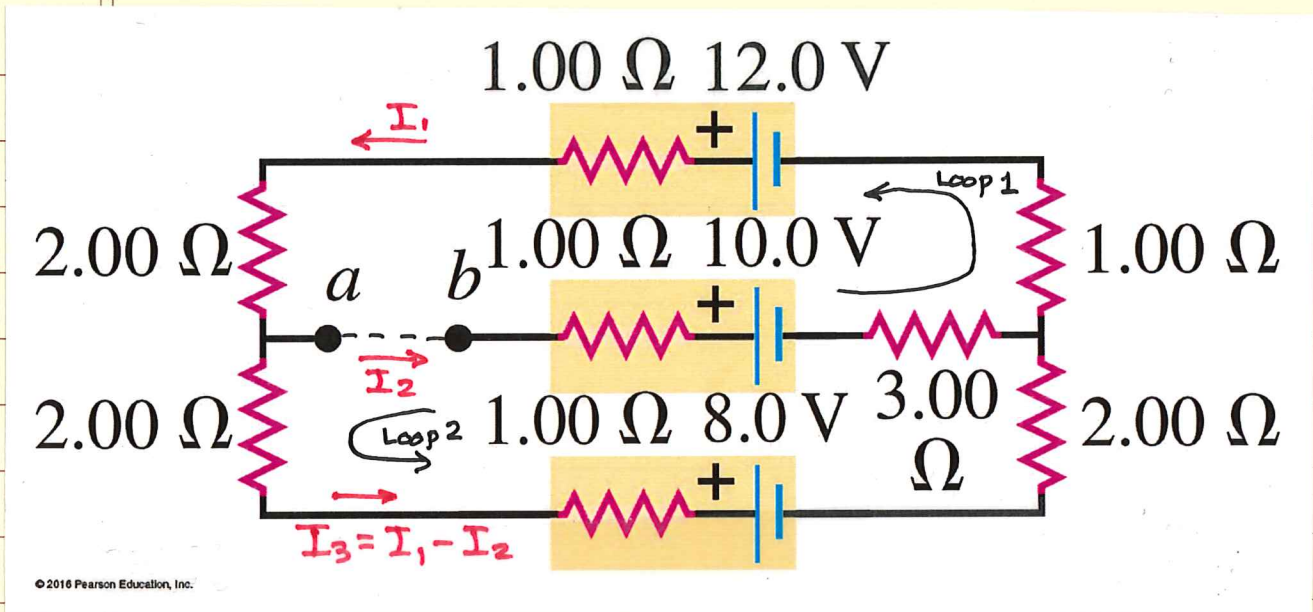
$$I = \frac{4}{9} \text{ A}$$

Upper Path

$$V_b - 10V + 12V - (4\Omega)I = V_a$$

$$V_a - V_b = 2V - (4\Omega)\frac{4}{9} \text{ A} = \frac{2}{9} \text{ volts}$$

$$V_{ab} = \frac{2}{9} \text{ volts}$$



b.) Points a and b are connected. Find $I_3 = I_1 - I_2$

$$\textcircled{1} \quad \sum V_i = -10\text{V} + 12\text{V} - (4\Omega)I_2 - (4\Omega)I_1 = 0$$

$$2\text{V} = 4I_1 + 4I_2$$

$$\textcircled{2} \quad \sum V_i = -8\text{V} + 10\text{V} - (5\Omega)(I_1 - I_2) + (4\Omega)I_2 = 0$$

$$- (5\Omega)I_1 + (9\Omega)I_2 = -2\text{V}$$

$$\textcircled{1} \quad 4I_1 + 4I_2 = 2\text{V} \quad \times 9 \rightarrow \textcircled{1} \quad 36I_1 + 36I_2 = 18\text{V}$$

$$\textcircled{2} \quad 5I_1 - 9I_2 = 2\text{V} \quad \times 4 \rightarrow \textcircled{2} \quad 20I_1 - 36I_2 = 8\text{V}$$

$$\text{Add} \rightarrow 56I_1 = 26\text{V}$$

$$I_1 = \frac{26\text{V}}{56\Omega} = \frac{13}{28}\text{A} = 0.4643\text{A}$$

$$\textcircled{1} \quad I_2 = \frac{2\text{V} - 4\left(\frac{13}{28}\text{A}\right)}{4} = 0.0357\text{A}$$

$$I_3 = I_1 - I_2 = 0.4286\text{A}$$