

## Homework Assignment #3

**Due Date: January 30, 2018 (Tuesday)**

In these problems, when the problem asks for mass, energy, and momentum, please write your answers in units of:

**Mass**  $\rightarrow MeV/c^2$  not kilograms !!

**Momentum**  $\rightarrow MeV/c$  not kilograms·meters/sec !!

**Energy**  $\rightarrow MeV$  not joules !!

unless otherwise specified.

When you are asked for velocities, always quote your answers in units of “c,” the speed of light—unless otherwise specified.

$$\text{velocity} = \beta c$$

**Problems: From “Modern Physics” by Kenneth Krane**

**2.12** Emission lines from a distant galaxy

**2.13** Physics professor goes through a “red light” because it appears “green.”

**2.17** A neutral K meson at rest decays into two  $\pi$  mesons, which travel in opposite directions along the x axis with speeds of  $0.828 c$ .

**2.18** A rod in the reference frame of observer  $O$  makes an angle of  $31^\circ$  . . .

**2.23 (modified)** Suppose Amelia travels at a speed of  $0.60c$  to a star that (according to Casper on Earth) is 8.0 light-years away. Upon her arrival to the star, she immediately jumps back into a space ship traveling  $0.60c$  towards earth. Upon her arrival at Earth, (a) what is Amelia’s age? And (b) What is Casper’s age? ***Please include a space-time diagram illustrating the world lines for Amelia and Casper.***

**Problem 6:** The kinetic energy of a proton in the LHC is 7.0 TeV and its  $\beta$  value is very very close to unity. Find how close by making an explicit calculation of  $1 - \beta$ .

**Problem 7:** (Extra Credit—2 points) A particle of mass  $M$  at rest decays into two unequal masses  $m_1$  and  $m_2$ . Show that the square of the momentum of each of the final particles is given by:

$$p^2 = \frac{[M^2 - (m_1 + m_2)^2][M^2 - (m_1 - m_2)^2]}{4M^2} c^2$$